

1. Record Nr.	UNISA996466377803316
Autore	Yengui Ihsen
Titolo	Constructive Commutative Algebra [[electronic resource]] : Projective Modules Over Polynomial Rings and Dynamical Gröbner Bases // by Ihsen Yengui
Pubbl/distr/stampa	Cham : , : Springer International Publishing : , : Imprint : Springer, , 2015
ISBN	3-319-19494-1
Edizione	[1st ed. 2015.]
Descrizione fisica	1 online resource (VII, 271 p. 5 illus.)
Collana	Lecture Notes in Mathematics, , 0075-8434 ; ; 2138
Disciplina	512.4
Soggetti	Commutative algebra Commutative rings Mathematical logic Computer science—Mathematics Commutative Rings and Algebras Mathematical Logic and Foundations Symbolic and Algebraic Manipulation
Lingua di pubblicazione	Inglese
Formato	Materiale a stampa
Livello bibliografico	Monografia
Note generali	Bibliographic Level Mode of Issuance: Monograph
Nota di contenuto	Projective modules over polynomial rings -- Dynamical Gröbner bases -- Syzygies in polynomial rings over valuation domains -- Exercises -- Detailed solutions to the exercises.
Sommario/riassunto	The main goal of this book is to find the constructive content hidden in abstract proofs of concrete theorems in Commutative Algebra, especially in well-known theorems concerning projective modules over polynomial rings (mainly the Quillen-Suslin theorem) and syzygies of multivariate polynomials with coefficients in a valuation ring. Simple and constructive proofs of some results in the theory of projective modules over polynomial rings are also given, and light is cast upon recent progress on the Hermite ring and Gröbner ring conjectures. New conjectures on unimodular completion arising from our constructive approach to the unimodular completion problem are presented. Constructive algebra can be understood as a first preprocessing step for computer algebra that leads to the discovery of general algorithms,

even if they are sometimes not efficient. From a logical point of view, the dynamical evaluation gives a constructive substitute for two highly nonconstructive tools of abstract algebra: the Law of Excluded Middle and Zorn's Lemma. For instance, these tools are required in order to construct the complete prime factorization of an ideal in a Dedekind ring, whereas the dynamical method reveals the computational content of this construction. These lecture notes follow this dynamical philosophy.
