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 6.4. Recurrence Relations

## Sommario/riassunto

This book gives an introduction to the classical, well-known special functions which play a role in mathematical physics, especially in boundary value problems. Calculus and complex function theory form the basis of the book and numerous formulas are given. Particular attention is given to asymptotic and numerical aspects of special functions, with numerous references to recent literature provided.