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Autore	Guille-Biel Winder Claire
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### Sommario/riassunto

This book explores the interconnections between tangible space, graphical space, and geometrical space, particularly in educational contexts. It delves into the theoretical and practical aspects of geometric learning, from middle school to kindergarten, emphasizing the role of figure restoration and the use of geometric tools. The authors, Claire Guille-Biel Winder and Teresa Assude, aim to enhance understanding and teaching of geometry by exploring different dimensions of space and incorporating modern educational practices such as coding. The book targets educators and researchers in mathematics education, providing insights into geometric drawing, the axiomatic foundations of geometry, and the integration of coding in teaching geometry.

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