1. Record Nr. UNINA9911019991303321 Autore Lui S. H (Shaun H.), <1961-> Titolo Numerical analysis of partial differential equations / / S.H. Lui Pubbl/distr/stampa Hoboken, N.J., : Wiley, c2011 **ISBN** 9786613282774 9781283282772 1283282771 9781118111116 1118111117 9781118111130 1118111133 9781118111109 1118111109 Descrizione fisica 1 online resource (508 p.) Pure and applied mathematics: a Wiley series of texts, monographs, Collana and tracts MAT034000 Classificazione Disciplina 518.64 518/.64 Soggetti Differential equations, Partial - Numerical solutions Variational inequalities (Mathematics) Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Description based upon print version of record. Note generali Includes bibliographical references and index. Nota di bibliografia Nota di contenuto Numerical Analysis of Partial Differential Equations; Contents; Preface; Acknowledgments; 1 Finite Difference; 1.1 Second-Order Approximation for : 1.2 Fourth-Order Approximation for : 1.3 Neumann Boundary Condition: 1.4 Polar Coordinates: 1.5 Curved Boundary; 1.6 Difference Approximation for 2; 1.7 A Convection-Diffusion Equation; 1.8 Appendix: Analysis of Discrete Operators; 1.9 Summary and Exercises; 2 Mathematical Theory of Elliptic PDEs; 2.1 Function Spaces; 2.2 Derivatives; 2.3 Sobolev Spaces; 2.4 Sobolev Embedding Theory; 2.5 Traces; 2.6 Negative Sobolev Spaces 2.7 Some Inequalities and Identities 2.8 Weak Solutions; 2.9 Linear Elliptic PDEs; 2.10 Appendix: Some Definitions and Theorems; 2.11

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Sommario/riassunto

A balanced guide to the essential techniques for solving elliptic partial differential equations Numerical Analysis of Partial Differential Equations provides a comprehensive, self-contained treatment of the quantitative methods used to solve elliptic partial differential equations (PDEs), with a focus on the efficiency as well as the error of the presented methods. The author utilizes coverage of theoretical PDEs, along with the nu merical solution of linear systems and various examples and exercises, to supply readers with an introduction to the essential concepts in the num