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Sommario/riassunto

"The celebrated Zariski Cancellation Problem asks as to when the existence of an isomorphism $X \times \mathbb{A}^1 \cong X \times \mathbb{A}^n$ for (affine) algebraic varieties X and X implies that $X \cong \mathbb{A}^n$. In this paper we provide a criterion for cancellation by the affine line (that is, $n = 1$) in the case where X is a normal affine surface admitting an \mathbb{A}^1 -fibration $X \rightarrow B$ with no multiple fiber over a smooth affine curve B . For two such surfaces $X \rightarrow B$ and $X' \rightarrow B$ we give a criterion as to when the cylinders $X \times \mathbb{A}^1$ and $X' \times \mathbb{A}^1$ are isomorphic over B . The latter criterion is expressed in terms of linear equivalence of certain divisors on the Danielewski-Fieseler quotient of X over B . It occurs that for a smooth \mathbb{A}^1 -fibered surface $X \rightarrow B$ the cancellation by the affine line holds if and only if $X \rightarrow B$ is a line bundle, and, for a normal such X , if and only if $X \rightarrow B$ is a cyclic quotient of a line bundle (an orbifold line bundle). If X does not admit any \mathbb{A}^1 -fibration over an affine base then the cancellation by the affine line is known to hold for X by a result of Bandman and Makar-Limanov. If the cancellation does not hold then X deforms in a non-isotrivial family of \mathbb{A}^1 -fibered surfaces B with cylinders \mathbb{A}^1 isomorphic over B . We construct such versal deformation families and their coarse moduli spaces provided B does not admit nonconstant invertible functions. Each of these coarse moduli spaces has infinite number of irreducible components of growing dimensions; each component is an affine variety with quotient singularities. Finally, we analyze from our viewpoint the examples of non-cancellation constructed by Danielewski, tom Dieck, Wilkens, Masuda and Miyanishi, e.a."