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**Sommario/riassunto**

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A comprehensive overview of the challenges in signal, data and pattern analysis in speech recognition, computational linguistics, image analysis and computer vision. Includes numerous exercises, an extensive bibliography, and additional resources -- extended proofs, selected solutions and examples -- on a companion website.

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