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Functions -- The Church-Turing Thesis -- Turing Machines -- Exercises -- 10 Universal Machines and Undecidability -- Universal Machines -- The Halting Problem -- The Undecidability of Validity -- Index Sets -- The Recursion Theorem -- Exercises.
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