1. Record Nr. UNINA9910829976203321 Autore Stankoviac Radomir S. **Titolo** Fourier analysis on finite groups with applications in signal processing and system design / / Radomir S. Stankoviac, Claudio Moraga, Jaakko Astola Piscataway, New Jersey:,: IEEE Press,, c2005 Pubbl/distr/stampa [Piscataqay, New Jersey]:,: IEEE Xplore,, [2005] **ISBN** 1-280-27793-9 9786610277933 0-471-74543-X 1-60119-376-9 0-471-74542-1 Descrizione fisica 1 online resource (262 p.) Altri autori (Persone) MoragaClaudio AstolaJaakko T Disciplina 621.3822 621.38220151 Soggetti Signal processing - Mathematics Fourier analysis Non-Abelian groups Lingua di pubblicazione Inglese **Formato** Materiale a stampa Monografia Livello bibliografico Note generali Description based upon print version of record. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto Preface -- Acknowledgments -- Acronyms -- 1 Signals and Their Mathematical Models -- 1.1 Systems -- 1.2 Signals -- 1.3 Mathematical Models of Signals -- References -- 2 Fourier Analysis --2.1 Representations of Groups -- 2.1.1 Complete Reducibility -- 2.2 Fourier Transform on Finite Groups -- 2.3 Properties of the Fourier Transform -- 2.4 Matrix Interpretation of the Fourier Transform on Finite Non-Abelian Groups -- 2.5 Fast Fourier Transform on Finite Non-Abelian Groups -- References -- 3 Matrix Interpretation of the

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Sommario/riassunto

Discover applications of Fourier analysis on finite non-Abelian groups
The majority of publications in spectral techniques consider Fourier
transform on Abelian groups. However, non-Abelian groups provide
notable advantages in efficient implementations of spectral methods.
Fourier Analysis on Finite Groups with Applications in Signal Processing
and System Design examines aspects of Fourier analysis on finite nonAbelian groups and discusses different methods used to determine
compact representations for discrete functions providing for their
efficient realizations and related applications. Switching functions are
included as an example of discrete functions in engineering practice.
Additionally, consideration is given to the polynomial expressions and
decision diagrams defined in terms of Fourier transform on finite nonAbelian groups. A solid foundation of this complex topic is provided by
beginning with a review of signals and their mathematical models and

Fourier analysis. Next, the book examines recent achievements and discoveries in: Matrix interpretation of the fast Fourier transform. Optimization of decision diagrams. Functional expressions on quaternion groups. Gibbs derivatives on finite groups. Linear systems on finite non-Abelian groups. Hilbert transform on finite groups Among the highlights is an in-depth coverage of applications of abstract harmonic analysis on finite non-Abelian groups in compact representations of discrete functions and related tasks in signal processing and system design, including logic design. All chapters are self-contained, each with a list of references to facilitate the development of specialized courses or self-study. With nearly 100 illustrative figures and fifty tables, this is an excellent textbook for graduate-level students and researchers in signal processing, logic design, and system theory-as well as the more general topics of computer science and applied mathematics.