1. Record Nr. UNINA9910825910603321 Autore Pajitnov Andrei V **Titolo** Circle-valued Morse theory [[electronic resource] /] / Andrei V. Pajitnov Berlin; ; New York, : De Gruyter, c2006 Pubbl/distr/stampa **ISBN** 1-282-19426-7 9786612194269 3-11-019797-9 Descrizione fisica 1 online resource (464 pages) Collana De Gruyter studies in mathematics., 0179-0986; 32 Classificazione SK 350 514/.74 Disciplina Soggetti Morse theory Manifolds (Mathematics) Lingua di pubblicazione Inglese Materiale a stampa **Formato** Livello bibliografico Monografia Description based upon print version of record. Note generali Nota di bibliografia Includes bibliographical references (p. [437]-444) and index. Front matter -- Contents -- Preface -- Introduction -- Part 1. Morse Nota di contenuto functions and vector fields on manifolds -- CHAPTER 1. Vector fields and C0 topology -- CHAPTER 2. Morse functions and their gradients --CHAPTER 3. Gradient flows of real-valued Morse functions -- Part 2. Transversality, handles, Morse complexes -- CHAPTER 4. The Kupka-Smale transversality theory for gradient flows -- CHAPTER 5. Handles -- CHAPTER 6. The Morse complex of a Morse function -- Part 3. Cellular gradients -- CHAPTER 7. Condition (C) -- CHAPTER 8. Cellular gradients are C0-generic -- CHAPTER 9. Properties of cellular gradients -- Part 4. Circle-valued Morse maps and Novikov complexes --CHAPTER 10. Completions of rings, modules and complexes --CHAPTER 11. The Novikov complex of a circle-valued Morse map --CHAPTER 12. Cellular gradients of circle-valued Morse functions and the Rationality Theorem -- CHAPTER 13. Counting closed orbits of the gradient flow -- CHAPTER 14. Selected topics in the Morse-Novikov theory -- Backmatter Sommario/riassunto In the early 1920's M. Morse discovered that the number of critical points of a smooth function on a manifold is closely related to the topology of the manifold. This became a starting point of the Morse

theory which is now one of the basic parts of differential topology.

Circle-valued Morse theory originated from a problem in

hydrodynamics studied by S. P. Novikov in the early 1980's. Nowadays, it is a constantly growing field of contemporary mathematics with applications and connections to many geometrical problems such as Arnold's conjecture in the theory of Lagrangian intersections, fibrations of manifolds over the circle, dynamical zeta functions, and the theory of knots and links in the three-dimensional sphere. The aim of the book is to give a systematic treatment of geometric foundations of the subject and recent research results. The book is accessible to first year graduate students specializing in geometry and topology.