Record Nr. UNINA9910816883003321 Autore Lan Kai-Wen Titolo Arithmetic compactifications of PEL-type Shimura varieties / / Kai-Wen Lan Princeton, NJ,: Princeton University Press, 2013 Pubbl/distr/stampa **ISBN** 1-299-33300-1 1-4008-4601-3 Edizione [Course Book] Descrizione fisica 1 online resource (588 p.) Collana London Mathematical Society monographs;; Vol. 36 Classificazione SK 240 Disciplina 516.3/5 Soggetti Shimura varieties Arithmetical algebraic geometry Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Description based upon print version of record. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto Frontmatter -- Contents -- Acknowledgments -- Introduction --Chapter One. Definition of Moduli Problems -- Chapter Two. Representability of Moduli Problems -- Chapter Three. Structures of Semi-Abelian Schemes -- Chapter Four. Theory of Degeneration for Polarized Abelian Schemes -- Chapter Five. Degeneration Data for Additional Structures -- Chapter Six. Algebraic Constructions of Toroidal Compactifications -- Chapter Seven. Algebraic Constructions of Minimal Compactifications -- Appendix A. Algebraic Spaces and Algebraic Stacks -- Appendix B. Deformations and Artin's Criterion --Bibliography -- Index By studying the degeneration of abelian varieties with PEL structures. Sommario/riassunto this book explains the compactifications of smooth integral models of all PEL-type Shimura varieties, providing the logical foundation for several exciting recent developments. The book is designed to be accessible to graduate students who have an understanding of schemes and abelian varieties. PEL-type Shimura varieties, which are natural generalizations of modular curves, are useful for studying the arithmetic properties of automorphic forms and automorphic representations, and they have played important roles in the development of the Langlands program. As with modular curves, it is

> desirable to have integral models of compactifications of PEL-type Shimura varieties that can be described in sufficient detail near the

boundary. This book explains in detail the following topics about PEL-type Shimura varieties and their compactifications: A construction of smooth integral models of PEL-type Shimura varieties by defining and representing moduli problems of abelian schemes with PEL structures An analysis of the degeneration of abelian varieties with PEL structures into semiabelian schemes, over noetherian normal complete adic base rings A construction of toroidal and minimal compactifications of smooth integral models of PEL-type Shimura varieties, with detailed descriptions of their structure near the boundary Through these topics, the book generalizes the theory of degenerations of polarized abelian varieties and the application of that theory to the construction of toroidal and minimal compactifications of Siegel moduli schemes over the integers (as developed by Mumford, Faltings, and Chai).