1. Record Nr. UNINA9910816414903321 Autore Reilly Norman R. Titolo Introduction to applied algebraic systems / / Norman R. Reilly Pubbl/distr/stampa New York, New York:,: Oxford University Press,, 2009 ©2009 **ISBN** 0-19-772720-4 0-19-970992-0 Descrizione fisica 1 online resource (xiii, 509 p.): ill Disciplina 512/.482 Soggetti Algebra Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Formerly CIP. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto CONTENTS; 1. Modular Arithmetic; 1.1 Sets, functions, numbers; 1.2 Induction; 1.3 Divisibility; 1.4 Prime Numbers; 1.5 Relations and Partitions; 1.6 Modular Arithmetic; 1.7 Equations in Zn; 1.8 Bar codes; 1.9 The Chinese Remainder Theorem: 1.10 Euler's '-function: 1.11 Theorems of Euler and Fermat; 1.12 Public Key Cryptosystems; 2. Rings and Fields; 2.1 Basic Properties; 2.2 Subrings and Subfields; 2.3 Review of Vector Spaces; 2.4 Polynomials; 2.5 Polynomial Evaluation and Interpolation; 2.6 Irreducible Polynomials; 2.7 Construction of Finite Fields; 2.8 Extension Fields; 2.9 Multiplicative Structure of Finite Fields: 2.10 Primitive Elements: 2.11 Subfield Structure of Finite Fields: 2.12 Minimal Polynomials; 2.13 Isomorphisms Between Fields; 2.14 Error Correcting Codes; 3. Groups and Permutations; 3.1 Basic Properties: 3.2 Subgroups: 3.3 Permutation Groups: 3.4 Matrix Groups:

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Sommario/riassunto

This resource provides a rigorous and extensive undergraduate introduction to algebraic systems covering basic number theory, rings, fields, polynomial theory, groups, algebraic geometry and elliptic curves.