Record Nr. UNINA9910814895903321 Autore Simon Barry <1946-> Titolo Szego's theorem and its descendants: spectral theory for L2 perturbations of orthogonal polynomials / / Barry Simon Princeton, N.J.,: Princeton University Press, 2010 Pubbl/distr/stampa **ISBN** 1-282-82115-6 9786612821158 1-4008-3705-7 Edizione [Course Book] Descrizione fisica 1 online resource (663 p.) Collana Porter Lectures;;6 Classificazione SK 680 Disciplina 515/.55 Soggetti Spectral theory (Mathematics) Orthogonal polynomials Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Description based upon print version of record. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto Frontmatter -- Contents -- Preface -- Chapter One. Gems of Spectral Theory -- Chapter Two. Szeg's Theorem -- Chapter Three The Killip-Simon Theorem: Szeg for OPRL -- Chapter Four. Sum Rules and Consequences for Matrix Orthogonal Polynomials -- Chapter Five. Periodic OPRL -- Chapter Six. Toda Flows and Symplectic Structures --Chapter Seven. Right Limits -- Chapter Eight. Szeg and Killip-Simon Theorems for Periodic OPRL -- Chapter Nine. Szeg's Theorem for Finite Gap OPRL -- Chapter Ten. A.C. Spectrum for Bethe-Cayley Trees -- Bibliography -- Author Index -- Subject Index Sommario/riassunto This book presents a comprehensive overview of the sum rule approach to spectral analysis of orthogonal polynomials, which derives from Gábor Szego's classic 1915 theorem and its 1920 extension. Barry Simon emphasizes necessary and sufficient conditions, and provides mathematical background that until now has been available only in journals. Topics include background from the theory of meromorphic functions on hyperelliptic surfaces and the study of covering maps of the Riemann sphere with a finite number of slits removed. This allows

for the first book-length treatment of orthogonal polynomials for

addition to the Szego and Killip-Simon theorems for orthogonal

measures supported on a finite number of intervals on the real line. In

polynomials on the unit circle (OPUC) and orthogonal polynomials on the real line (OPRL), Simon covers Toda lattices, the moment problem, and Jacobi operators on the Bethe lattice. Recent work on applications of universality of the CD kernel to obtain detailed asymptotics on the fine structure of the zeros is also included. The book places special emphasis on OPRL, which makes it the essential companion volume to the author's earlier books on OPUC.