1. Record Nr. UNINA9910814096803321 Autore Farmakis Ioannis **Titolo** Fixed point theorems and their applications / / Ioannis Farmakis, Martin Moskowitz, City University of New York, USA Pubbl/distr/stampa New Jersey: .: World Scientific, . [2013] 2013 **ISBN** 981-4458-92-9 Descrizione fisica 1 online resource (xi, 234 pages): illustrations Collana Gale eBooks Disciplina 515.7248 Soggetti Fixed point theory Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Description based upon print version of record. Includes bibliographical references and index. Nota di bibliografia Contents: Preface and Acknowledgments: Introduction: 1 Early Fixed Nota di contenuto Point Theorems; 1.1 The Picard-Banach Theorem; 1.2 Vector Fields on Spheres; 1.3 Proof of the Brouwer Theorem and Corollaries; 1.3.1 A Counter Example: 1.3.2 Applications of the Brouwer Theorem: 1.3.3 The Perron-Frobenius Theorem; 1.3.4 Google; A Billion Dollar Fixed Point Theorem; 1.4 Fixed Point Theorems for Groups of Affine Maps of Rn; 1.4.1 Affine Maps and Actions; 1.4.2 Affine Actions of Non Compact Groups; 2 Fixed Point Theorems in Analysis; 2.1 The Schauder-Tychonoff Theorem 2.1.1 Proof of the Schauder-Tychonoff Theorem 2.2 Applications of the Schauder-Tychonoff Theorem; 2.3 The Theorems of Hahn, Kakutani and Markov-Kakutani; 2.4 Amenable Groups; 2.4.1 Amenable Groups; 2.4.2 Structure of Connected Amenable Lie Groups; 3 The Lefschetz Fixed Point Theorem; 3.1 The Lefschetz Theorem for Compact Polyhedra; 3.1.1 Projective Spaces; 3.2 The Lefschetz Theorem for a Compact Manifold: 3.2.1 Preliminaries from Differential Topology: 3.2.2 Transversality: 3.3 Proof of the Lefschetz Theorem: 3.4 Some Applications: 3.4.1 Maximal Tori in Compact Lie Groups 3.4.2 The Poincare-Hopf's Index Theorem3.5 The Atiyah-Bott Fixed Point Theorem; 3.5.1 The Case of the de Rham Complex; 4 Fixed Point Theorems in Geometry; 4.1 Some Generalities on Riemannian

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## Sommario/riassunto

This is the only book that deals comprehensively with fixed point theorems overall of mathematics. Their importance is due, as the book demonstrates, to their wide applicability. Beyond the first chapter, each of the other seven can be read independently of the others so the reader has much flexibility to follow his/her own interests. The book is written for graduate students and professional mathematicians and could be of interest to physicists, economists and engineers.