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Characteristic 2; 6.5 Extraspecial 3-Groups; 6.6 Extraspecial 2-Groups of Small Order; 6.7 The Remaining Cases; 7. Reduced Pairs of Quasisimple Type; 7.1 Nonreal Reduced Pairs; 7.2 Regular Orbits; 7.3 Covering Numbers, Projective Marks; 7.4 Sporadic Groups; 7.5 Alternating Groups; 7.6 Linear Groups; 7.7 Symplectic Groups; 7.8 Unitary Groups; 7.9 Orthogonal Groups; 7.10 Exceptional Groups  
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Sommario/riassunto

The  $k(GV)$  conjecture claims that the number of conjugacy classes (irreducible characters) of the semidirect product  $GV$  is bounded above by the order of  $V$ . Here  $V$  is a finite vector space and  $G$  a subgroup of  $GL(V)$  of order prime to that of  $V$ . It may be regarded as the special case of Brauer's celebrated  $k(B)$  problem dealing with  $p$ -blocks  $B$  of  $p$ -solvable groups ( $p$  a prime). Whereas Brauer's problem is still open in its generality, the  $k(GV)$  problem has recently been solved, completing the work of a series of aut