

1. Record Nr.	UNINA9910789212503321
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Titolo	Group Theory and Its Applications in Physics [[electronic resource] /] / by Teturo Inui, Yukito Tanabe, Yositaka Onodera
Pubbl/distr/stampa	Berlin, Heidelberg : , : Springer Berlin Heidelberg : , : Imprint : Springer, , 1990
ISBN	3-642-80021-1
Edizione	[1st ed. 1990.]
Descrizione fisica	1 online resource (XV, 397 p.)
Collana	Springer Series in Solid-State Sciences, , 0171-1873 ; ; 78
Disciplina	530.1/522
Soggetti	Physics Crystallography Atoms Mathematical Methods in Physics Numerical and Computational Physics, Simulation Crystallography and Scattering Methods Atomic, Molecular, Optical and Plasma Physics
Lingua di pubblicazione	Inglese
Formato	Materiale a stampa
Livello bibliografico	Monografia
Note generali	"With 72 Figures."
Nota di bibliografia	Includes bibliographical references and index.
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Displacements -- 10.4.1 Kramers Degeneracy -- 11. Space Groups -- 11.1 Translational Symmetry of Crystals -- 11.2 Symmetry Operations in Space Groups -- 11.3 Structure of Space Groups -- 11.4 Bravais Lattices -- 11.5 Nomenclature of Space Groups -- 11.6 The Reciprocal Lattice and the Brillouin Zone -- 11.7 Irreducible Representations of the Translation Group... -- 11.8 The Group of the Wavevector  $k$  and Its Irreducible Representations -- 11.9 Irreducible Representations of a Space Group -- 11.10 Double Space Groups -- 12. Electronic States in Crystals -- 12.1 Bloch Functions and  $E(k)$  Spectra -- 12.2 Examples of Energy Bands: Ge and TlBr -- 12.3 Compatibility or Connectivity Relations -- 12.4 Bloch Functions Expressed in Terms of Plane Waves -- 12.5 Choice of the Origin -- 12.5.1 Effect of the Choice on Bloch Wavefunctions -- 12.6 Bloch Functions Expressed in Terms of Atomic Orbitals -- 12.7 Lattice Vibrations -- 12.8 The Spin-Orbit Interaction and Double Space Groups.... -- 12.9 Scattering of an Electron by Lattice Vibrations -- 12.10 Interband Optical Transitions -- 12.11 Frenkel Excitons in Molecular Crystals -- 12.12 Selection Rules in Space Groups -- 12.12.1 Symmetric and Antisymmetric Product Representations -- 13. Time Reversal and Nonunitary Groups -- 13.1 Time Reversal -- 13.2 Nonunitary Groups and Corepresentations -- 13.3 Criteria for Space Groups and Examples -- 13.4 Magnetic Space Groups -- 13.5 Excitons in Magnetic Compounds; Spin Waves -- 13.5.1 Symmetry of the Hamiltonian -- 14. Landau's Theory of Phase Transitions -- 14.1 Landau's Theory of Second-Order Phase Transitions -- 14.2 Crystal Structures and Spin Alignments -- 14.3 Derivation of the Lifshitz Criterion -- 14.3.1 Lifshitz's Derivation of the Lifshitz Criterion -- 15. The Symmetric Group -- 15.1 The Symmetric Group (Permutation Group) -- 15.2 Irreducible Characters -- 15.3 Construction of Irreducible Representation Matrices -- 15.4 The Basis for Irreducible Representations -- 15.5 The Unitary Group and the Symmetric Group -- 15.6 The Branching Rule -- 15.7 Wavefunctions for the Configuration  $(nl)^x$  -- 15.8  $D(J)$  as Irreducible Representations of  $SU(2)$  -- 15.9 Irreducible Representations of  $U(m)$  -- Appendices -- A. The Thirty-Two Crystallographic Point Groups -- B. Character Tables for Point Groups -- Answers and Hints to the Exercises -- Motifs of the Family Crests -- References.

## Sommario/riassunto

This book has been written to introduce readers to group theory and its applications in atomic physics, molecular physics, and solid-state physics. The first Japanese edition was published in 1976. The present English edition has been translated by the authors from the revised and enlarged edition of 1980. In translation, slight modifications have been made in Chaps. 8 and 14 to update and condense the contents, together with some minor additions and improvements throughout the volume. The authors cordially thank Professor J. L. Birman and Professor M. Cardona, who encouraged them to prepare the English translation. Tokyo, January 1990 T. Inui, Y. Tanabe, Y. Onodera

**Preface to the Japanese Edition** As the title shows, this book has been prepared as a textbook to introduce readers to the applications of group theory in several fields of physics. Group theory is, in a nutshell, the mathematics of symmetry. It has three main areas of application in modern physics. The first originates from early studies of crystal morphology and constitutes a framework for classical crystal physics. The analysis of the symmetry of tensors representing macroscopic physical properties (such as elastic constants) belongs to this category. The second area was enunciated by E. Wigner (1926) as a powerful means of handling quantum-mechanical problems and was first applied in this sense to the analysis of atomic spectra. Soon, H.

2. Record Nr.	UNICAMPANIAVAN00055551
Autore	Hochschild, Gerhard P.
Titolo	Basic theory of algebraic groups and Lie algebras / Gerhard P. Hochschild
Pubbl/distr/stampa	New York, : Springer, 1981
ISBN	03-87905-41-3 978-03-87905-41-9
Descrizione fisica	VIII, 267 p ; 23 cm
Soggetti	14L10 - Group varieties [MSC 2020] 14L35 - Classical groups (algebro-geometric aspects) [MSC 2020] 17B35 - Universal enveloping (super)algebras [MSC 2020] 17B45 - Lie algebras of linear algebraic groups [MSC 2020] 20-XX - Group theory and generalizations [MSC 2020] 20G05 - Representation theory for linear algebraic groups [MSC 2020] 20G10 - Cohomology theory for linear algebraic groups [MSC 2020] 20G15 - Linear algebraic groups over arbitrary fields [MSC 2020]
Lingua di pubblicazione	Inglese
Formato	Materiale a stampa
Livello bibliografico	Monografia