Record Nr. UNINA9910624377803321 Autore Steppeler Jurgen **Titolo** Mathematics of the weather: polygonal spline local-Galerkin methods on spheres / / Jurgen Steppeler and Jinxi Li Pubbl/distr/stampa Cham, Switzerland: ,: Springer, , [2022] ©2022 **ISBN** 3-031-07238-3 Descrizione fisica 1 online resource (328 pages) Collana Springer atmospheric sciences Disciplina 551.51011 Soggetti Atmospheric models Atmospheric models - Mathematics Physical geography Models matemàtics Geografia física Llibres electrònics Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Nota di bibliografia Includes bibliographical references (pages 311-316) and index. Nota di contenuto Intro -- Foreword -- Preface -- Acknowledgments -- Contents --Acronyms -- Introduction -- Numerics -- Discretization on Spherical Grids -- Efficiency of the Computational Grid -- Numerical Methods --Validations of Numerical Methods Using NWP Models -- Verifications of Numerical Methods for Climate Modeling -- Simple Finite Difference Procedures -- The Runge-Kutta and Other Time Discretization Schemes -- Homogeneous and Inhomogeneous Difference Schemes -- Some Further Properties of Finite Difference Schemes -- The Von Neumann Method of Stability Analysis -- Dynamic Equations of Toy Models --Diffusion -- The Boussinesq Model of Convection Between Heated Plates -- The Lorenz Paradigmatic Model -- Local-Galerkin Schemes in 1D -- Functional Representations, Amplitudes, and Basis Functions --The Classic Galerkin Procedure -- Spectral Elements -- The L-Galerkin

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