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Autore	Gryniewicz David J. <1978->
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Nota di contenuto	Intro -- Preface -- Contents -- 1 Introduction -- 1.1 Convex Geometry -- 1.2 Krull Domains, Transfer Krull Monoids and Factorization -- 1.3 Zero-Sum Sequences -- 1.4 Overview of Main Results -- 2 Preliminaries and General Notation -- 2.1 Convex Geometry -- 2.2 Lattices and Partially Ordered Sets -- 2.3 Sequences and Rational Sequences -- 2.4 Arithmetic Invariants for Transfer Krull Monoids -- 2.5 Asymptotic Notation -- 3 Asymptotically Filtered Sequences, Encasement and Boundedness -- 3.1 Asymptotically Filtered Sequences -- 3.2 Encasement and Boundedness -- 4 Elementary Atoms, Positive Bases and Reay Systems -- 4.1 Basic Non-degeneracy Characterizations -- 4.2 Elementary Atoms and Positive Bases -- 4.3 Reay Systems -- 4.4 -Filtered Sequences, Minimal Encasement and

Reay Systems -- 5 Oriented Reay Systems -- 6 Virtual Reay Systems --  
7 Finitary Sets -- 7.1 Core Definitions and Properties -- 7.2 Series  
Decompositions and Virtualizations -- 7.3 Finiteness Properties of  
Finitary Sets -- 7.4 Interchangeability and the Structure of  $X(G_0)$  -- 8  
Factorization Theory -- 8.1 Lambert Subsets and Elasticity -- 8.2 The  
Structure of Atoms and Arithmetic Invariants -- Summary -- 8.3  
Transfer Krull Monoids Over Subsets of Finitely Generated Abelian  
Groups -- Summary -- References -- Index.

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## Sommario/riassunto

This book develops a new theory in convex geometry, generalizing positive bases and related to Carathéodory's Theorem by combining convex geometry, the combinatorics of infinite subsets of lattice points, and the arithmetic of transfer Krull monoids (the latter broadly generalizing the ubiquitous class of Krull domains in commutative algebra) This new theory is developed in a self-contained way with the main motivation of its later applications regarding factorization. While factorization into irreducibles, called atoms, generally fails to be unique, there are various measures of how badly this can fail. Among the most important is the elasticity, which measures the ratio between the maximum and minimum number of atoms in any factorization. Having finite elasticity is a key indicator that factorization, while not unique, is not completely wild. Via the developed material in convex geometry, we characterize when finite elasticity holds for any Krull domain with finitely generated class group  $G$ , with the results extending more generally to transfer Krull monoids. This book is aimed at researchers in the field but is written to also be accessible for graduate students and general mathematicians.

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