Record Nr. UNINA9910586596303321 Operator and norm inequalities and related topics // Richard M. Aron **Titolo** [and three others], editors Pubbl/distr/stampa Cham, Switzerland:,: Springer Nature Switzerland AG,, [2022] ©2022 **ISBN** 3-031-02104-5 Descrizione fisica 1 online resource (822 pages) Collana Trends in mathematics 515.724 Disciplina Soggetti Operator theory Inequalities (Mathematics) Desigualtats (Matemàtica) Teoria d'operadors Llibres electrònics Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Nota di bibliografia Includes bibliographical references. Intro -- Preface -- Part I: Matrix and Operator Inequalities -- Part II: Nota di contenuto Orthogonality and Inequalities -- Part III: Inequalities Related to Types of Operators -- Part IV: Inequalities in Various Banach Spaces -- Part V: Inequalities in Commutative and Noncommutative Probability Spaces --Contents -- Part I Matrix and Operator Inequalities -- Log-majorization Type Inequalities -- 1 Introduction -- 2 Matrix Majorization -- 3 Trace and Determinantal Inequalities -- 4 Golden-Thompson Inequality and Araki's Log-majorization -- 5 Ando-Hiai Inequality -- 6 BLP and Matharu-Aujla Inequalities -- 7 Inequalities for Operator Connections -- 8 Ando and Visick's Inequalities for the Hadamard Product -- 9 Indefinite Inequalities -- References -- Ando-Hiai Inequality: Extensions and Applications -- 1 Introduction -- 2 Extensions -- 3 Applications -- 4 Concluding Remarks -- References -- Relative Operator Entropy -- 1 Introduction -- 2 Operator Means and Solidarities -- 3 Relative Operator Entropy -- 4 CPR Geometry -- 5

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