

1. Record Nr.	UNINA9910554280303321
Autore	Schilling Rene L.
Titolo	Brownian Motion : a guide to random processes and stochastic calculus with a chapter on simulation by bjorn bottcher // Rene L. Schilling
Pubbl/distr/stampa	Boston, Massachusetts : , : De Gruyter, , [2021] ©2021
ISBN	3-11-074127-X
Edizione	[Second edition.]
Descrizione fisica	1 online resource : illustrations
Collana	De Gruyter textbook
Classificazione	SK 820
Disciplina	519.233
Soggetti	Brownian motion processes Stochastic processes
Lingua di pubblicazione	Inglese
Formato	Materiale a stampa
Livello bibliografico	Monografia
Note generali	Includes bibliographical references and index.
Nota di contenuto	Intro -- Preface -- Contents -- Dependence chart -- 1 Robert Brown's new thing -- 2 Brownian motion as a Gaussian process -- 3 Constructions of Brownian motion -- 4 The canonical model -- 5 Brownian motion as a martingale -- 6 Brownian motion as a Markov process -- 7 Brownian motion and transition semigroups -- 8 The PDE connection -- 9 The variation of Brownian paths -- 10 Regularity of Brownian paths -- 11 Brownian motion as a random fractal -- 12 The growth of Brownian paths -- 13 Strassen's functional law of the iterated logarithm -- 14 Skorokhod representation -- 15 Stochastic integrals: $L_t$ -- $\sup_{t \geq 0} L_t$ -- $2L_t$ -- $\sup_{t \geq 0} 2L_t$ -- Theory -- 16 Stochastic integrals: localization -- 17 Stochastic integrals: martingale drivers -- 18 Itô's formula -- 19 Applications of Itô's formula -- 20 Wiener Chaos and iterated Wiener-Itô integrals -- 21 Stochastic differential equations -- 22 Stratonovich's stochastic calculus -- 23 On diffusions -- 24 Simulation of Brownian motion by Björn Böttcher -- A Appendix -- Bibliography -- Index.
Sommario/riassunto	Brownian motion is one of the most important stochastic processes in continuous time and with continuous state space. Within the realm of stochastic processes, Brownian motion is at the intersection of Gaussian processes, martingales, Markov processes, diffusions and random fractals, and it has influenced the study of these topics. Its central position within mathematics is matched by numerous

applications in science, engineering and mathematical finance. Often textbooks on probability theory cover, if at all, Brownian motion only briefly. On the other hand, there is a considerable gap to more specialized texts on Brownian motion which is not so easy to overcome for the novice. The authors' aim was to write a book which can be used as an introduction to Brownian motion and stochastic calculus, and as a first course in continuous-time and continuous-state Markov processes. They also wanted to have a text which would be both a readily accessible mathematical back-up for contemporary applications (such as mathematical finance) and a foundation to get easy access to advanced monographs. This textbook, tailored to the needs of graduate and advanced undergraduate students, covers Brownian motion, starting from its elementary properties, certain distributional aspects, path properties, and leading to stochastic calculus based on Brownian motion. It also includes numerical recipes for the simulation of Brownian motion.

---