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Nota di contenuto	I Foundations of Finsler Geometry -- 1. Warm-up: Norms and inner products -- 2. Finsler manifolds -- 3. Properties of geodesics -- 4. Covariant derivatives -- 5. Curvature -- 6. Examples of Finsler manifolds -- 7. Variation formulas for arclength -- 8. Some comparison theorems -- II Geometry and analysis of weighted Ricci curvature -- 9. Weighted Ricci curvature -- 10. Examples of measured Finsler manifolds -- 11. The nonlinear Laplacian -- 12. The Bochner-Weitzenböck formula -- 13. Nonlinear heat flow -- 14. Gradient estimates -- 15. Bakry-Ledoux isoperimetric inequality -- 16. Functional inequalities -- III Further topics -- 17. Splitting theorems -- 18. Curvature-dimension condition -- 19. Needle decompositions.
Sommario/riassunto	This monograph presents recent developments in comparison geometry and geometric analysis on Finsler manifolds. Generalizing the weighted Ricci curvature into the Finsler setting, the author systematically derives the fundamental geometric and analytic inequalities in the Finsler context. Relying only upon knowledge of differentiable manifolds, this treatment offers an accessible entry point to Finsler geometry for readers new to the area. Divided into three parts, the book begins by establishing the fundamentals of Finsler

geometry, including Jacobi fields and curvature tensors, variation formulas for arc length, and some classical comparison theorems. Part II goes on to introduce the weighted Ricci curvature, nonlinear Laplacian, and nonlinear heat flow on Finsler manifolds. These tools allow the derivation of the Bochner–Weitzenböck formula and the corresponding Bochner inequality, gradient estimates, Bakry–Ledoux’s Gaussian isoperimetric inequality, and functional inequalities in the Finsler setting. Part III comprises advanced topics: a generalization of the classical Cheeger–Gromoll splitting theorem, the curvature-dimension condition, and the needle decomposition. Throughout, geometric descriptions illuminate the intuition behind the results, while exercises provide opportunities for active engagement. Comparison Finsler Geometry offers an ideal gateway to the study of Finsler manifolds for graduate students and researchers. Knowledge of differentiable manifold theory is assumed, along with the fundamentals of functional analysis. Familiarity with Riemannian geometry is not required, though readers with a background in the area will find their insights are readily transferrable.
