1. Record Nr. UNINA9910480724803321 Autore Kato Tosio <1917-> Titolo Perturbation Theory for Linear Operators [[electronic resource] /] / by Tosio Kato Pubbl/distr/stampa Berlin, Heidelberg:,: Springer Berlin Heidelberg:,: Imprint: Springer, 1995 **ISBN** 3-642-66282-X Edizione [2nd ed. 1995.] Descrizione fisica 1 online resource (XXI, 623 p.) Collana ;;132 Disciplina 515/.7246 Soggetti Partial differential equations Calculus of variations Partial Differential Equations Calculus of Variations and Optimal Control; Optimization Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia "With 3 Figures." Note generali Nota di bibliografia Includes bibliographical references and indexes. Nota di contenuto One Operator theory in finite-dimensional vector spaces -- § 1. Vector spaces and normed vector spaces -- § 2. Linear forms and the adjoint space -- § 3. Linear operators -- § 4. Analysis with operators -- § 5. The eigenvalue problem -- § 6. Operators in unitary spaces -- Two Perturbation theory in a finite-dimensional space -- § 1. Analytic perturbation of eigenvalues -- § 2. Perturbation series -- § 3. Convergence radii and error estimates -- § . Similarity transformations of the eigenspaces and eigenvectors -- § 5. Non-analytic perturbations -- § 6. Perturbation of symmetric operators -- Three Introduction to the theory of operators in Banach spaces -- § 1. Banach spaces -- § 2. Linear operators in Banach spaces -- § 3. Bounded operators -- § 4. Compact operators -- § 5. Closed operators -- § 6. Resolvents and

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## Sommario/riassunto

In view of recent development in perturbation theory, supplementary notes and a supplementary bibliography are added at the end of the new edition. Little change has been made in the text except that the para- graphs V-§ 4.5, VI-§ 4.3, and VIII-§ 1.4 have been completely rewritten, and a number of minor errors, mostly typographical, have been corrected. The author would like to thank many readers who brought the errors to his attention. Due to these changes, some theorems, lemmas, and formulas of the first edition are missing from the new edition while new ones are added. The new ones have numbers different from those attached to the old ones which they may have replaced. Despite considerable expansion, the bibliography i" not intended to be complete. Berkeley, April 1976 ToslO RATO Preface to the First Edition This book is intended to give a systematic presentation of perturba- tion theory for linear operators. It is hoped that the book will be useful to students as well as to mature scientists, both in mathematics and in the physical sciences.