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1.

	 Basic Constructions of Topoi 1. Lawvere-Tierney Topologies 2. Sheaves 3. The Associated Sheaf Functor 4. Lawvere-Tierney Subsumes Grothendieck 5. Internal Versus External 6. Group Actions 7. Category Actions 8. The Topos of Coalgebras 9. The Filter-Quotient Construction Exercises VI. Topoi and Logic 1. The Topos of Sets 2. The Cohen Topos 3. The Preservation of Cardinal Inequalities 4. The Axiom of Choice 5. The Mitchell-Bénabou Language 6. Kripke-Joyal Semantics 7. Sheaf Semantics 8. Real Numbers in a Topos 9. Brouwer's Theorem: All Functions are Continuous 10. Topos-Theoretic and Set-Theoretic Foundations Exercises VII. Geometric Morphisms 1. Geometric Morphisms and Basic Examples 2. Tensor Products 3. Group Actions 4. Embeddings and Surjections 5. Points 6. Filtering Functors 7. Morphisms into Grothendieck Topoi 8. Filtering Functors 10. Morphisms Between Sites Exercises VIII. Classifying Topoi 1. Classifying Spaces in Topology 2. Torsors 3. Classifying Topoi 4. The Object Classifier 5. The Classifying Topos for Rings 6. The Zariski Topos Classifies Local Rings 7. Simplicial Sets 8. Simplicial Sets Classify Linear Orders Exercises 1X. Localic Topoi 1. Locales 2. Points and Sober Spaces 3. Spaces from Locales 4. Embeddings and Surjections of Locales 5. Localic Topoi 6. Open Geometric Morphisms 7. Open Maps of Locales 8. Open Maps and Sites 9. The Diaconescu Cover and Barr's Theorem 10. The Stone Space of a Complete Boolean Algebra 11. Deligne's Theorem Exercises X. Geometric Logic and Classifying Topoi 1. First-Order Theories 2. Models in Topoi 3. Geometric Theories 4. Categories of Definable Objects 5. Syntactic Sites 6. The Classifying Topos of a Geometric Theories 4.
Sommario/riassunto	We dedicate this book to the memory of J. Frank Adams. His clear insights have inspired many mathematicians, including both of us. In January 1989, when the first draft of our book had been completed, we heard the sad news of his untimely death. This has cast a shadow on our subsequent work. Our views of topos theory, as presented here, have been shaped by continued study, by conferences, and by many personal contacts with friends and colleagues-including especially O. Bruno, P. Freyd, J.M.E. Hyland, P.T. Johnstone, A. Joyal, A. Kock, F.W. Lawvere, G.E. Reyes, R Solovay, R Swan, RW. Thomason, M. Tierney, and G.C. Wraith. Our presentation combines ideas and results from these people and from many others, but we have not endeavored to specify the various original sources. Moreover, a number of people have assisted in our work by pro- viding helpful comments on portions of the manuscript. In this respect, we extend our hearty thanks in particular to P. Corazza, K. Edwards, J. Greenlees, G. Janelidze, G. Lewis, and S. Schanuel.