1. Record Nr. UNINA9910453742903321 Autore Barbeau Edward <1938-> Titolo Mathematical fallacies, flaws, and flimflam / / Edward J. Barbeau Washington, DC:,: Mathematical Association of America,, 2000 Pubbl/distr/stampa **ISBN** 1-61444-518-4 Descrizione fisica 1 online resource (184 p.) Collana Spectrum series 510 Disciplina Soggetti Mathematics Mathematics - Study and teaching Electronic books. Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Description based upon print version of record. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto ""copyright page ""; ""title page ""; ""FOREWORD""; ""Contents""; ""1 NUMBERS""; ""1. How to get drunk and rich at the same time""; ""2. Fifty per cent more for fifty per cent less""; ""3. Whose real world?""; ""4. United in purpose""; ""5. A case of black and white---but not so much black""; ""6. Effects of changing temperature""; ""7. To those that have shall be given""; ""8. Distributing addition over multiplication""; ""9. Distributing exponents over sums"; ""10. An exponential mess""; ""11. A product of logarithms""; ""12. A divisibility property""; ""13. All perfect numbers are even"" ""14. Why Wiles' proof of the Fermat Conjecture is false""""15. A quick (?) proof of irrationality""; ""16. A rational combination of two transcendentals""; ""17. How the factorial works""; ""Dollars and sense""; ""2 ALGEBRA AND TRIGONOMETRY""; ""1. Do you know how to split the atom?""; ""2. The number of tickets""; ""3. A superficial volume problem""; ""4. The end justifies the means""; ""5. How to solve a quadratic equation""; ""6. A new method for solving a cubic""; ""7. An old method for solving a cubic""; ""8. An exponential equation""; ""9. Logarithms distribute over sums"" ""10. The multiplication rules for logarithms"""11. A lack of technical unanimity""; ""12. A straightforward cancellation""; ""13. An application of the Cauchy-Schwarz Inequality""; ""14. Surprising symmetry""; ""15. Factoring homogeneous polynomials""; ""16. Polynomial detection"";

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Sommario/riassunto

Through hard experience, mathematicians have learned to subject even the most evident assertions to rigorous scrutiny, as intuition and facile reasoning can often lead them astray. However, the impossibility and impracticality of completely watertight arguments make it possible for errors to slip by the most watchful eye. They are often subtle and difficult of detection. When found, they can teach us a lot and can present a real challenge to straighten out. Presenting students with faulty arguments to troubleshoot can be an effective way of helping them critically understand material, and it is for this reason that I began to compile fallacies and publish them first in the Notes of the Canadian Mathematical Society and later in the College Mathematics Journal in the Fallacies, Flaws and Flimflam section. I hoped to challenge and amuse readers, as well as to provide them with material suitable for teaching and student assignments. This book collects the items from the first eleven years of publishing in the CMJ. One source of such errors is the work of students. Occasionally, a text book will weigh in with a specious result or solution. Nonprofessional sources, such as newspapers, are responsible for a goodly number of mishaps, particularly in arithmetic (especially percentages) and probability; their use in classrooms may help students become critical readers and listeners of the media. Quite a few items come from professional mathematicians. The reader will find in this book some items that are not erroneous but seem to be. These need a fuller analysis to clarify the situation. All the items are presented for your entertainment and use. The mathematical topics covered include algebra, trigonometry, geometry, probability, calculus, linear algebra, and modern algebra.