

1. Record Nr.	UNINA9910349324903321
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Titolo	Discrete Energy on Rectifiable Sets // by Sergiy V. Borodachov, Douglas P. Hardin, Edward B. Saff
Pubbl/distr/stampa	New York, NY : , : Springer New York : , : Imprint : Springer, , 2019
ISBN	9780387848082 0387848088
Edizione	[1st ed. 2019.]
Descrizione fisica	1 online resource (xviii, 666 pages) : illustrations
Collana	Springer Monographs in Mathematics, , 2196-9922
Disciplina	518.25
Soggetti	Convex geometry Discrete geometry Mathematical physics Measure theory Number theory Topology Computer science - Mathematics Convex and Discrete Geometry Mathematical Methods in Physics Measure and Integration Number Theory Mathematical Applications in Computer Science
Lingua di pubblicazione	Inglese
Formato	Materiale a stampa
Livello bibliografico	Monografia
Nota di contenuto	0. An Overview: Discretizing Manifolds via Particle Interactions.-1. Preliminaries -- 2. Basics of Minimal Energy -- 3.-Introduction to Packing and Covering -- 4. Continuous and Discrete Energy -- 5. LP Bounds on the Sphere -- 6. Asymptotics for Energy Minimizing Congurations on S_d -- 7. Some Popular Algorithms for Distributing Points on S^2 -- 8. Minimal Energy in the Hypersingular Case -- 9. Minimal Energy Asymptotics in the "Harmonic Series" Case -- 10. Periodic Riesz Energy -- 11. Congurations with non-Uniform Distribution -- 12. Low Complexity Energy Methods for Discretization -- 13. Best-Packing on Compact Sets -- 14. Optimal Discrete Measures

Sommario/riassunto

This book aims to provide an introduction to the broad and dynamic subject of discrete energy problems and point configurations. Written by leading authorities on the topic, this treatise is designed with the graduate student and further explorers in mind. The presentation includes a chapter of preliminaries and an extensive Appendix that augments a course in Real Analysis and makes the text self-contained. Along with numerous attractive full-color images, the exposition conveys the beauty of the subject and its connection to several branches of mathematics, computational methods, and physical/biological applications. This work is destined to be a valuable research resource for such topics as packing and covering problems, generalizations of the famous Thomson Problem, and classical potential theory in \mathbb{R}^d . It features three chapters dealing with point distributions on the sphere, including an extensive treatment of Delsarte–Yudin–Levenshtein linear programming methods for lower bounding energy, a thorough treatment of Cohn–Kumar universality, and a comparison of 'popular methods' for uniformly distributing points on the two-dimensional sphere. Some unique features of the work are its treatment of Gauss-type kernels for periodic energy problems, its asymptotic analysis of minimizing point configurations for non-integrable Riesz potentials (the so-called Poppy-seed bagel theorems), its applications to the generation of non-structured grids of prescribed densities, and its closing chapter on optimal discrete measures for Chebyshev (polarization) problems. .
