1. Record Nr. UNINA9910300141703321 Autore Nazaikinskii Vladimir **Titolo** The localization problem in index theory of elliptic operators / / by Vladimir Nazaikinskii, Bert-Wolfgang Schulze, Boris Sternin Basel:,: Springer Basel:,: Imprint: Birkhäuser,, 2014 Pubbl/distr/stampa **ISBN** 3-0348-0510-1 Edizione [1st ed. 2014.] Descrizione fisica 1 online resource (122 p.) Pseudo-Differential Operators, Theory and Applications, , 2297-0355; Collana ; 10 515.7242 Disciplina Soggetti Global analysis (Mathematics) Manifolds (Mathematics) K-theory Functional analysis Differential equations, Partial Global Analysis and Analysis on Manifolds K-Theory **Functional Analysis** Partial Differential Equations Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Description based upon print version of record. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto Preface -- Introduction -- 0.1 Basics of Elliptic Theory -- 0.2 Surgery and the Superposition Principle -- 0.3 Examples and Applications --0.4 Bibliographical Remarks -- Part I: Superposition Principle -- 1 Superposition Principle for the Relative Index -- 1.1 Collar Spaces --1.2 Proper Operators and Fredholm Operators -- 1.3 Superposition Principle -- 2 Superposition Principle for K-Homology -- 2.1 Preliminaries -- 2.2 Fredholm Modules and K-Homology -- 2.3 Superposition Principle -- 2.4 Fredholm Modules and Elliptic Operators -- 3 Superposition Principle for KK-Theory -- 3.1 Preliminaries -- 3.2 Hilbert Modules, Kasparov Modules, and KK -- 3.3 Superposition

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Sommario/riassunto

This book deals with the localization approach to the index problem for elliptic operators. Localization ideas have been widely used for solving various specific index problems for a long time, but the fact that there is actually a fundamental localization principle underlying all these solutions has mostly passed unnoticed. The ignorance of this general principle has often necessitated using various artificial tricks and hindered the solution of important new problems in index theory. So far, the localization principle has scarcely been covered in journal papers. The present book is intended to fill this gap. Both the general localization principle and its applications to specific problems, old and new, are covered. Concisely and clearly written, this monograph includes numerous figures helping the reader to visualize the material. The Localization Problem in Index Theory of Elliptic Operators will be of interest to researchers as well as graduate and postgraduate students specializing in differential equations and related topics.