1. Record Nr. UNINA9910300105103321 Autore Ohsawa Takeo Titolo L<sup>2</sup> Approaches in Several Complex Variables: Towards the Oka-Cartan Theory with Precise Bounds / / by Takeo Ohsawa Tokyo:,: Springer Japan:,: Imprint: Springer,, 2018 Pubbl/distr/stampa 4-431-56852-2 **ISBN** Edizione [2nd ed. 2018.] Descrizione fisica 1 online resource (267 pages) Collana Springer Monographs in Mathematics, , 1439-7382 Disciplina 515.94 Soggetti Functions of complex variables Algebraic geometry Differential geometry Functional analysis Several Complex Variables and Analytic Spaces Algebraic Geometry **Differential Geometry Functional Analysis** Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Nota di contenuto Part I Holomorphic Functions and Complex Spaces -- Convexity Notions -- Complex Manifolds -- Classical Questions of Several Complex Variables -- Part II The Method of L<sup>2</sup> Estimates -- Basics of Hilbert Space Theory -- Harmonic Forms -- Vanishing Theorems --Finiteness Theorems -- Notes on Complete Kahler Domains (= CKDs) -- Part III L2 Variant of Oka-Cartan Theory -- Extension Theorems --Division Theorems -- Multiplier Ideals -- Part IV Bergman Kernels --The Bergman Kernel and Metric -- Bergman Spaces and Associated Kernels -- Sequences of Bergman Kernels -- Parameter Dependence --Part V L<sup>2</sup> Approaches to Holomorphic Foliations -- Holomorphic Foliation and Stable Sets -- L2 Method Applied to Levi Flat Hypersurfaces -- LFHs in Tori and Hopf Surfaces. Sommario/riassunto This monograph presents the current status of a rapidly developing part of several complex variables, motivated by the applicability of

effective results to algebraic geometry and differential geometry.

Special emphasis is put on the new precise results on the L<sup>2</sup> extension

of holomorphic functions in the past 5 years. In Chapter 1, the classical questions of several complex variables motivating the development of this field are reviewed after necessary preparations from the basic notions of those variables and of complex manifolds such as holomorphic functions, pseudoconvexity, differential forms, and cohomology. In Chapter 2, the L2 method of solving the d-bar equation is presented emphasizing its differential geometric aspect. In Chapter 3, a refinement of the Oka-Cartan theory is given by this method. The L<sup>2</sup> extension theorem with an optimal constant is included, obtained recently by Z. Bocki and separately by Q.-A. Guan and X.-Y. Zhou. In Chapter 4, various results on the Bergman kernel are presented. including recent works of Maitani-Yamaguchi, Berndtsson, Guan-Zhou, and Berndtsson-Lempert. Most of these results are obtained by the L2 method. In the last chapter, rather specific results are discussed on the existence and classification of certain holomorphic foliations and Levi flat hypersurfaces as their stables sets. These are also applications of the L<sup>2</sup> method obtained during the past 15 years.