Record Nr.	UNINA9910299782503321
Autore	Möller Manfred
Titolo	Spectral Theory of Operator Pencils, Hermite-Biehler Functions, and their Applications / / by Manfred Möller, Vyacheslav Pivovarchik
Pubbl/distr/stampa	Cham : , : Springer International Publishing : , : Imprint : Birkhäuser, , 2015
ISBN	3-319-17070-8
Edizione	[1st ed. 2015.]
Descrizione fisica	1 online resource (418 p.)
Collana	Operator Theory: Advances and Applications, , 0255-0156 ; ; 246
Disciplina	515.7222
Soggetti	Operator theory Differential equations Mathematical physics Operator Theory Ordinary Differential Equations Mathematical Physics
Lingua di pubblicazione	Inglese
Formato	Materiale a stampa
Livello bibliografico	Monografia
Note generali	Description based upon print version of record.
Nota di bibliografia	Includes bibliographical references and indexes.
Nota di contenuto	Preface Part I: Operator Pencils 1.Quadratic Operator Pencils 2. Applications of Quadratic Operator Pencils 3.Operator Pencils with Essential Spectrum 4.Operator Pencils with a Gyroscopic Term Part II: Hermite-Biehler Functions 5.Generalized Hermite-Biehler Functions 6.Applications of Shifted Hermite-Biehler Functions Part III: Direct and Inverse Problems 7.Eigenvalue Asymptotics 8. Inverse Problems Part IV: Background Material 9.Spectral Dependence on a Parameter 10.Sobolev Spaces and Differential Operators 11.Analytic and Meromorphic Functions 12.Inverse Sturm-Liouville Problems Bibliography Index Index of Notation.
Sommario/riassunto	The theoretical part of this monograph examines the distribution of the spectrum of operator polynomials, focusing on quadratic operator polynomials with discrete spectra. The second part is devoted to applications. Standard spectral problems in Hilbert spaces are of the form A-I for an operator A, and self-adjoint operators are of particular interest and importance, both theoretically and in terms of

1.

applications. A characteristic feature of self-adjoint operators is that their spectra are real, and many spectral problems in theoretical physics and engineering can be described by using them. However, a large class of problems, in particular vibration problems with boundary conditions depending on the spectral parameter, are represented by operator polynomials that are quadratic in the eigenvalue parameter and whose coefficients are self-adjoint operators. The spectra of such operator polynomials are in general no more real, but still exhibit certain patterns. The distribution of these spectra is the main focus of the present volume. For some classes of quadratic operator polynomials, inverse problems are also considered. The connection between the spectra of such quadratic operator polynomials and generalized Hermite-Biehler functions is discussed in detail. Many applications are thoroughly investigated, such as the Regge problem and damped vibrations of smooth strings, Stieltjes strings, beams, star graphs of strings and quantum graphs. Some chapters summarize advanced background material, which is supplemented with detailed proofs. With regard to the reader's background knowledge, only the basic properties of operators in Hilbert spaces and well-known results from complex analysis are assumed.