Record Nr. UNINA9910299768903321 Autore Lowen R Titolo Index analysis: approach theory at work / / by R. Lowen Pubbl/distr/stampa London:,: Springer London:,: Imprint: Springer,, 2015 **ISBN** 1-4471-6485-7 Edizione [1st ed. 2015.] Descrizione fisica 1 online resource (477 p.) Springer Monographs in Mathematics, , 1439-7382 Collana Disciplina 514.325 Soggetti Geometry Algebra Ordered algebraic structures Approximation theory Functional analysis **Topology Probabilities** Order, Lattices, Ordered Algebraic Structures Approximations and Expansions **Functional Analysis** Probability Theory and Stochastic Processes Lingua di pubblicazione Inglese **Formato** Materiale a stampa Monografia Livello bibliografico Note generali Description based upon print version of record. Includes bibliographical references and index. Nota di bibliografia Nota di contenuto Approach spaces -- Topological and metric approach spaces --Approach invariants -- Index analysis -- Uniform gauge spaces --Extensions of spaces and morphisms -- Approach theory meets Topology -- Approach theory meets Functional analysis -- Approach theory meets Probability -- Approach theory meets Hyperspaces --Approach theory meets DCPO's and Domains -- Categorical considerations. Sommario/riassunto A featured review of the AMS describes the author's earlier work in the field of approach spaces as, 'A landmark in the history of general

topology'. In this book, the author has expanded this study further and taken it in a new and exciting direction. The number of conceptually and technically different systems which characterize approach spaces is

increased and moreover their uniform counterpart, uniform gauge

spaces, is put into the picture. An extensive study of completions, both for approach spaces and for uniform gauge spaces, as well as compactifications for approach spaces is performed. A paradigm shift is created by the new concept of index analysis. Making use of the rich intrinsic quantitative information present in approach structures, a technique is developed whereby indices are defined that measure the extent to which properties hold, and theorems become inequalities involving indices; therefore vastly extending the realm of applicability of many classical results. The theory is then illustrated in such varied fields as topology, functional analysis, probability theory, hyperspace theory and domain theory. Finally a comprehensive analysis is made concerning the categorical aspects of the theory and its links with other topological categories. Index Analysis will be useful for mathematicians working in category theory, topology, probability and statistics, functional analysis, and theoretical computer science.