1. Record Nr. UNINA9910163942603321 Autore Isett Philip Titolo Hölder Continuous Euler Flows in Three Dimensions with Compact Support in Time / / Philip Isett Pubbl/distr/stampa Princeton, NJ:,: Princeton University Press,, [2017] ©2017 **ISBN** 1-4008-8542-6 Descrizione fisica 1 online resource (214 pages) Collana Annals of Mathematics Studies:: 357 Disciplina 532/.05 Soggetti Fluid dynamics - Mathematics Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Previously issued in print: 2017. Includes bibliographical references and index. Nota di bibliografia Frontmatter -- Contents -- Preface -- Part I. Introduction -- Part II. Nota di contenuto General Considerations of the Scheme -- Part III. Basic Construction of the Correction -- Part IV. Obtaining Solutions from the Construction --Part V. Construction of Regular Weak Solutions: Preliminaries -- Part VI Construction of Regular Weak Solutions: Estimating the Correction --Part VII. Construction of Regular Weak Solutions: Estimating the New Stress -- Acknowledgments -- Appendices -- References -- Index Sommario/riassunto Motivated by the theory of turbulence in fluids, the physicist and chemist Lars Onsager conjectured in 1949 that weak solutions to the incompressible Euler equations might fail to conserve energy if their spatial regularity was below 1/3-Hölder. In this book, Philip Isett uses the method of convex integration to achieve the best-known results regarding nonuniqueness of solutions and Onsager's conjecture. Focusing on the intuition behind the method, the ideas introduced now play a pivotal role in the ongoing study of weak solutions to fluid dynamics equations. The construction itself-an intricate algorithm with hidden symmetries-mixes together transport equations, algebra, the method of nonstationary phase, underdetermined partial differential equations (PDEs), and specially designed high-frequency waves built using nonlinear phase functions. The powerful "Main Lemma"-used here to construct nonzero solutions with compact support in time and to prove nonuniqueness of solutions to the initial value problem-has

been extended to a broad range of applications that are surveyed in the

appendix. Appropriate for students and researchers studying nonlinear PDEs, this book aims to be as robust as possible and pinpoints the main difficulties that presently stand in the way of a full solution to Onsager's conjecture.