1. Record Nr. UNINA9910148978503321

Autore Kobayashi Toshiyuki

Titolo Conformal Symmetry Breaking Operators for Differential Forms on

Spheres / / by Toshiyuki Kobayashi, Toshihisa Kubo, Michael Pevzner

Pubbl/distr/stampa Singapore:,: Springer Singapore:,: Imprint: Springer,, 2016

ISBN 981-10-2657-2

Edizione [1st ed. 2016.]

Descrizione fisica 1 online resource (IX, 192 p.)

Collana Lecture Notes in Mathematics, , 0075-8434;; 2170

Disciplina 515.7242

Soggetti Geometry, Differential

Topological groups

Lie groups

Mathematical physics

Fourier analysis

Differential equations, Partial

Differential Geometry

Topological Groups, Lie Groups

Mathematical Physics

Fourier Analysis

Partial Differential Equations

Lingua di pubblicazione Inglese

Formato Materiale a stampa

Livello bibliografico Monografia

Note generali Includes index.

Sommario/riassunto This work is the first systematic study of all possible conformally

covariant differential operators transforming differential forms on a Riemannian manifold X into those on a submanifold Y with focus on the model space (X, Y) = (Sn, Sn-1). The authors give a complete classification of all such conformally covariant differential operators, and find their explicit formulæ in the flat coordinates in terms of basic operators in differential geometry and classical hypergeometric polynomials. Resulting families of operators are natural generalizations of the Rankin–Cohen brackets for modular forms and Juhl's operators from conformal holography. The matrix-valued factorization identities

among all possible combinations of conformally covariant differential

operators are also established. The main machinery of the proof relies on the "F-method" recently introduced and developed by the authors. It is a general method to construct intertwining operators between C-induced representations or to find singular vectors of Verma modules in the context of branching rules, as solutions to differential equations on the Fourier transform side. The book gives a new extension of the F-method to the matrix-valued case in the general setting, which could be applied to other problems as well. This book offers a self-contained introduction to the analysis of symmetry breaking operators for infinite-dimensional representations of reductive Lie groups. This feature will be helpful for active scientists and accessible to graduate students and young researchers in differential geometry, representation theory, and theoretical physics.