1. Record Nr. UNINA9910139005203321 Autore Janssen Jacques Titolo Applied diffusion processes from engineering to finance [[electronic resource] /] / Jacques Janssen, Oronzio Manca, Raimando Manca London, : Wiley, 2013 Pubbl/distr/stampa **ISBN** 1-118-57833-3 1-118-57834-1 1-299-47558-2 1-118-57668-3 Descrizione fisica 1 online resource (411 p.) Collana **ISTE** Altri autori (Persone) MancaOronzio MancaRaimondo Disciplina 519.233 Soggetti **Business mathematics** Differential equations, Partial Diffusion processes **Engineering mathematics** Lingua di pubblicazione Inglese **Formato** Materiale a stampa Livello bibliografico Monografia Note generali Description based upon print version of record. Nota di contenuto Title Page; Contents; Introduction; Chapter 1. Diffusion Phenomena and Models; 1.1. General presentation of diffusion process; 1.2. General balance equations; 1.3. Heat conduction equation; 1.4. Initial and boundary conditions; Chapter 2. Probabilistic Models of Diffusion Processes; 2.1. Stochastic differentiation; 2.1.1. Definition; 2.1.2. Examples: 2.2. Ito's formula: 2.2.1. Stochastic differential of a product: 2.2.2. Ito's formula with time dependence; 2.2.3. Interpretation of Ito's formula; 2.2.4. Other extensions of Ito's formula; 2.3. Stochastic differential equations (SDE) 2.3.1. Existence and unicity general theorem (Gikhman and Skorokhod [GIK 68])2.3.2. Solution of SDE under the canonical form; 2.4. Ito and diffusion processes: 2.4.1. Ito processes: 2.4.2. Diffusion processes: 2.4.3. Kolmogorov equations; 2.5. Some particular cases of diffusion processes; 2.5.1. Reduced form; 2.5.2. The OUV (Ornstein-Uhlenbeck-Vasicek) SDE; 2.5.3. Solution of the SDE of Black-Scholes-Samuelson;

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## Sommario/riassunto

The aim of this book is to promote interaction between engineering, finance and insurance, as these three domains have many models and methods of solution in common for solving real-life problems. The authors point out the strict inter-relations that exist among the diffusion models used in engineering, finance and insurance. In each of the three fields, the basic diffusion models are presented and their strong similarities are discussed. Analytical, numerical and Monte Carlo simulation methods are explained with a view to applying them to obtain the solutions to the different problems pres