1. Record Nr. UNINA9910136914703321 Autore Celant Giorgio **Titolo** Interpolation and extrapolation optimal designs 1: polynomial regression and approximation theory / / Giorgio Celant, Michel Broniatowski London, England; ; Hoboken, New Jersey:,: iSTE:,: Wiley,, 2016 Pubbl/distr/stampa ©2016 **ISBN** 1-119-29229-8 1-119-29228-X Descrizione fisica 1 online resource (266 p.) Collana Mathematics and Statistics Disciplina 511.42 Soggetti Interpolation Approximation theory Lingua di pubblicazione Inglese **Formato** Materiale a stampa Monografia Livello bibliografico Note generali Description based upon print version of record. Nota di bibliografia Includes bibliographical references and index. Nota di contenuto Table of Contents; Title; Copyright; Preface; Introduction; I.1. The scope of this book; I.2. A generic case: the Hoel and Levine extrapolation scheme and the uniform interpolation design of Guest; I. 3. Extrapolation design in non standard cases, algorithms; I.4. Uniform approximation of functions, an outlook; I.5. A general bibliography; PART 1: Elements from Approximation Theory; 1 Uniform Approximation; 1.1. Canonical polynomials and uniform approximation; 1.2. Existence of the best approximation; 1.3. Characterization and uniqueness of the best approximation 2 Convergence Rates for the Uniform Approximation and Algorithms2. 1. Introduction; 2.2. The Borel-Chebyshev theorem and standard functions; 2.3. Convergence of the minimax approximation; 2.4. Proof of the de la Vallee Poussin theorem; 2.5. The Yevgeny Yakovlevich

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